

## Homework 1 (due Monday 10 September)

Exercise 5:1

- 5:1. Show that the following functions are primitive recursive.

(a) Multiplication:  $x \cdot y$  [10 pts]

(b) Exponentiation  $x^y$  [10 pts]

(c) Factorial  $x!$  [10 pts]

(d) Monus  $x \dot{-} y$  defined by

$$x \dot{-} y := \begin{cases} x - y & \text{if } x \geq y \\ 0 & \text{if } x < y \end{cases}$$

[10 pts]

(OPTIONAL) Conclude that the primitive recursive relations are closed under conjunction. [10 pts]